

# Modeling analysis of the influence of plasticity on high pressure deformation of hcp-Co

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(Received 8 September 2008)

Previously measured *in situ* x-ray diffraction is used to assess the development of internal elastic strains within grains of a sample of polycrystalline cobalt plastically deformed up to a pressure of 42.6 GPa. An elastoplastic self-consistent polycrystal model is used to simulate the macroscopic flow curves and internal strain development within the sample. Input parameters are single-crystal elastic moduli and their pressure dependence, critical resolved shear stresses, and hardening behavior of the slip and twinning mechanisms which are active in Co crystals. At 42 GPa, the differential stress in hcp-Co is  $1.9 \pm 0.1$  GPa. The comparison between experimental and predicted data leads us to conclude that: (a) plastic relaxation plays a primary role in controlling the evolution and ordering of the lattice strains; (b) the plastic behavior of hcp-Co deforming under high pressure is controlled by basal and prismatic slip of  $\langle a \rangle$  dislocations, and either pyramidal slip of  $\langle c+a \rangle$  dislocations, or compressive twinning, or both. Basal slip is by far the easiest and most active deformation mechanism. Elastoplastic self-consistent models are shown to overcome the limitations of models based on continuum elasticity theory for the interpretation of x-ray diffraction data measured on stressed samples. They should be used for the interpretation of these experiments.

DOI: XXXX

PACS number(s): 62.50.-p, 62.20.-x, 91.60.-x, 61.05.cp

## I. INTRODUCTION

Characterizing the effect of pressure on elastic and plastic properties of condensed matter is particularly important for understanding elasticity, mechanical stability of solids, material strength, interatomic interactions, and phase-transition mechanisms. In particular, hexagonal-closed-packed (hcp) metals are of great interest because they tend to exhibit intriguing physical properties<sup>1-4</sup> that represent a challenge for first-principles calculations,<sup>5-8</sup> and also because the Earth's inner core could be mainly composed of the hcp polymorph of Fe,  $\epsilon$ -Fe.<sup>9</sup>

In the past few years, techniques have been developed to study the plastic properties of materials *in situ* under combined high pressure and high temperature.<sup>10-13</sup> In those experiments x-ray diffraction is used to probe stress and lattice preferred orientations (LPOs) within the sample and extract physical properties such as dominant deformation mechanisms, flow laws, or ultimate stress. However, the theory commonly used for relating the measured lattice strains to stress and elastic properties<sup>14</sup> is based on lower or upper bound assumptions and has shown severe limitations. In particular, it was shown that this model yields inconsistent results for inverting single-crystal elastic properties for  $\epsilon$ -Fe.<sup>15-18</sup> This was also confirmed by extensive work on hcp-Co which demonstrated that the method provides elastic moduli that are inconsistent with those provided by a range of other experimental and theoretical techniques.<sup>3,5,19-23</sup>

In the material science community, the issue of stress measurement using x-ray or neutron diffraction is known as residual stress analysis.<sup>24,25</sup> There is a body of work showing

that the analysis of such data is not straightforward.<sup>26-30</sup> Indeed, stress and strain are very heterogeneous in plastically deformed materials and upper or lower bound models based on continuum elasticity theory do not account for this phenomenon. Various techniques have been developed for the interpretation of experimental data, based on self-consistent methods,<sup>26,31</sup> or finite-element modeling.<sup>28</sup> Self-consistent analysis has already been applied to high pressure solids with a cubic structure<sup>32,33</sup> and to trigonal quartz.<sup>34</sup>

Here, we look at the plastic properties of hcp Co under pressure. Cobalt lies next to iron in the Periodic Table and its hcp phase has a wide stability field.<sup>35</sup> Unlike the hcp phase of iron, it is stable at ambient pressure with readily available single crystals. As such, it has become a paradigm for comparing and testing numerous high pressure techniques. The phase diagram and equation of state have been studied using both x-ray diffraction<sup>35-37</sup> and first-principles calculations.<sup>5,8</sup> Elastic properties have been obtained under ambient pressure using ultrasonic techniques<sup>38</sup> and at high pressure using inelastic x-ray scattering<sup>19,20,39</sup> (IXS), Raman spectroscopy,<sup>3</sup> impulsive stimulated light scattering,<sup>23</sup> and first-principles techniques.<sup>5</sup> The plastic properties of hcp-Co have been investigated under ambient pressure for both coarse grains<sup>40-44</sup> and nanocrystalline samples.<sup>45-47</sup> High pressure diamond-anvil cell (DAC) radial diffraction (RDX) experiments have been reported,<sup>22</sup> but lacked an interpretation based on the interplay between elastic and plastic mechanisms.

In this paper, we use a modification of the elastoplastic self-consistent (EPSC) model of Turner and Tomé<sup>31</sup> to simulate and interpret DAC experiment previously done on a Co aggregate for pressures up to 42.6 GPa.<sup>22</sup> This model yields

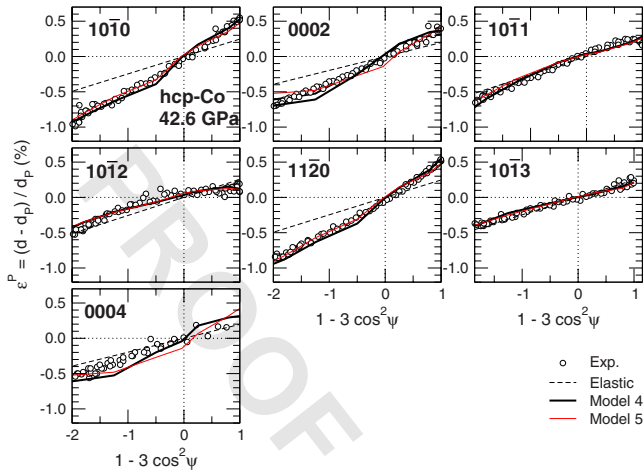


FIG. 1. (Color online) Measured and simulated strains vs  $(1-3 \cos^2 \psi)$  under the hydrostatic pressure of 42.6 GPa. Circles are data from Ref. 22.  $d$  are measured  $d$  spacings and  $d_P$   $d$  spacings under equivalent hydrostatic pressure. Thick black lines are results of EPSC calculations using model 4 in Table II. Thin red lines are results of EPSC calculations using model 5 in Table II. Thin dashed lines are predictions of an elastic model with no effect of LPO (Ref. 14) assuming a differential stress of 4 GPa. In all cases, the  $d$  spacings under equivalent hydrostatic pressure  $d_P$  have been obtained assuming relation 15.

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86 information about the absolute strength of the deformation  
87 mechanisms involved, stress distribution among grains in the  
88 sample, and true stress values for the polycrystal. In addition,  
89 our modeling shows the important role that plastic relaxation  
90 and nonhomogeneity of stress and strain play in high pres-  
91 sure experiments.

## 92 II. METHODS

### 93 A. Experimental data

94 The experimental data on hcp-Co that we use here have  
95 been published previously.<sup>22</sup> Two experiments were per-  
96 formed in which a sample of pure hcp-Co was compressed in  
97 a diamond-anvil cell, up to 42.6 GPa for the first run and up  
98 to 12.8 GPa for the second run. Diffraction data were col-  
99 lected in a radial geometry with the incoming x-ray beam  
100 perpendicular to the load axis.

101 Figure 1 shows measured strains for several crystallo-  
102 graphic planes vs  $(1-3 \cos^2 \psi)$  for a hydrostatic pressure of  
103 42.6 GPa, where  $\psi$  is the angle between the diffracting plane  
104 normal and the direction of maximum stress. They are nearly  
105 linear with  $(1-3 \cos^2 \psi)$ , as predicted by purely elastic lat-  
106 tice strain theory.<sup>14</sup> However, it was shown that stresses cal-  
107 culated using this theory for individual lattice planes were  
108 inconsistent.<sup>22</sup>

109 For all pressures in the experiment, the variations in dif-  
110 fraction intensity with orientation were used to extract lattice  
111 preferred orientations in the sample, while peak shifts were  
112 used to extract lattice strains parameters  $Q$  (discussed in Sec.  
113 II B 4) for the  $10\bar{1}0$ ,  $0002$ ,  $10\bar{1}1$ ,  $10\bar{1}2$ ,  $11\bar{2}0$ ,  $10\bar{1}3$ , and  
114  $0004$  diffraction lines of hcp-Co (Fig. 2).

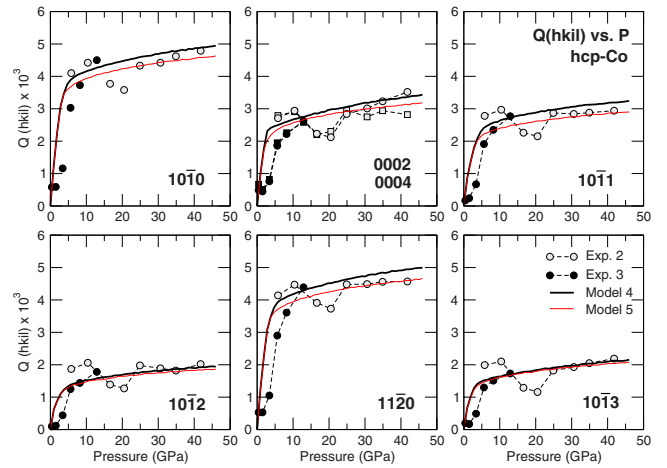


FIG. 2. (Color online) Measured and simulated lattice strain parameters vs pressure for the  $10\bar{1}0$ ,  $0002$ ,  $0004$ ,  $10\bar{1}1$ ,  $10\bar{1}2$ ,  $11\bar{2}0$ , and  $10\bar{1}3$  diffraction lines of hcp-Co. Gray symbols are data from Exp. 2 in Ref. 22, solid symbols are data from Exp. 3 in Ref. 22, thick black lines are EPSC simulations using model 4 in Table II, and thin red lines are EPSC simulations using model 5 in Table II. Experimental data for the  $0004$  diffraction line are shown using square symbols. All other experimental data are represented with circles.

## B. Elastic model

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### 1. Stress and strain

116

Under high pressure, it is preferable to separate the effect  
of hydrostatic pressure and deviatoric stress, and define elas-  
tic moduli as relating stress and strain deviations relative to  
the hydrostatic state. Elastic constants are then appropriate  
for calculation of elastic wave velocities and comparison  
with previous work. This relation is not trivial under  
pressure,<sup>48-50</sup> and we therefore discuss several definitions of  
stress and strains. In this paper, the superscript “0” will refer  
to absolute stress and strain (relative to ambient pressure),  
while the superscript “P” will refer to stress, strain, or stiff-  
ness relative to the state of hydrostatic pressure  $P$ .

The relation between stress tensors relative to ambient  
pressure (absolute stress)  $\sigma_{ij}^0$  and stress tensors relative to the  
hydrostatic pressure (relative stress)  $\sigma_{ij}^P$  is straightforward,

$$\sigma_{ij}^0 = \sigma_{ij}^P + P \cdot \delta_{ij} = C_{ijkl}^P \epsilon_{kl}^P + P \cdot \delta_{ij}, \quad (1)$$

where  $\delta_{ij}$  is the Kronecker function and  $\epsilon_{ij}^P$  the strain tensor  
relative to the state of hydrostatic pressure.  $\sigma_{ij}^P$  is often re-  
ferred to as deviatoric stress in the literature, although it may  
not be traceless at the grain level.  $C_{ijkl}^P$  are single-crystal  
elastic moduli for a medium under hydrostatic pressure  $P$ .

Strain definitions can be more complicated. If we consider  
an element of length  $d_0$  under ambient pressure, length  $d_P$  at  
the hydrostatic pressure  $P$ , and length  $d$  under a general  
stress  $\sigma_{ij}^0$ , we define the following lattice strains:

$$\epsilon^P = \frac{d - d_P}{d_P}, \quad (2)$$

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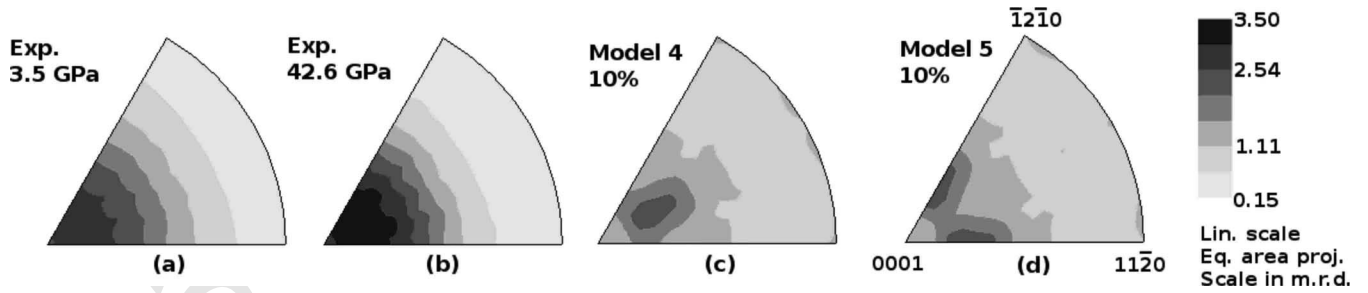


FIG. 3. [(a) and (b)] Experimental and [(c) and (d)] simulated inverse pole figures of the compression direction for hcp-Co. [(a) and (b)] Experimental data are from Exp. 2 in Ref. 22. Simulations are results of VPSC calculations using models (c) 4 and (d) 5 in Table II after 10% strain. Equal area projection, linear scale, and contours in m.r.d.

$$\epsilon^0 = \frac{d - d_0}{d_0}, \quad (3)$$

$$\epsilon_p^0 = \frac{d_p - d_0}{d_0}, \quad (4)$$

from where

$$\epsilon^0 = (1 + \epsilon_p^0)\epsilon^P + \epsilon_p^0. \quad (5)$$

$\epsilon^P$  are the strains relative to the hydrostatic pressure state and could be referred to as “relative strains;”  $\epsilon^0$  are the strains relative to the ambient pressure state and could be referred to as “absolute strains.”

Note that elastic moduli under hydrostatic pressure  $C_{ijkl}^P$  relate relative strains  $\epsilon_{ij}^P$  and relative stresses  $\sigma_{ij}^P$ , and that the relation between absolute strains  $\epsilon_{ij}^0$  and absolute stresses  $\sigma_{ij}^0$  is not straightforward.

### 2. Coordinate systems

Analysis and calculations can be simplified if single-crystal elastic moduli,  $d$  spacings measured using x-ray diffraction, and sample stress, are expressed in the suitable coordinate system.

The diamond-anvil cell geometry defines a sample coordinate system,  $K_S$ , with  $Z_S$  aligned with the compression direction and  $Y_S$  parallel to the incoming x-ray beam, pointing toward the detector. This coordinate system is well defined in the experiment and useful to relate all information expressed in the other systems. Stress in diamond-anvil cells are mostly axial and, when expressed in  $K_S$ , the stress applied to the polycrystalline sample reads

$$\sigma^{P-K_S} = \begin{bmatrix} -\frac{t}{3} & 0 & 0 \\ 0 & -\frac{t}{3} & 0 \\ 0 & 0 & 2\frac{t}{3} \end{bmatrix}, \quad (6)$$

where  $t$  is the differential stress.

The diffraction direction defines a diffraction coordinate system  $K_D$  with the axis  $Z_D$  parallel to the scattering vector  $\mathbf{N}$  (bisector between the incoming beam and the diffracted x-ray beam collected by the detector) and  $Y_D$  perpendicular to  $Z_D$  and contained in the plane defined by the incident and diffracted beams. In  $K_D$  the  $d$  spacings measured in diffraction are the 33 component of the crystal strain tensor

$$\epsilon_{33}^{P-K_D} = \frac{d_m(hkl) - d_p(hkl)}{d_p(hkl)}, \quad (7)$$

where  $d_m(hkl)$  is the measured  $d$  spacing for the  $hkl$  reflection and  $d_p(hkl)$  is the  $d$  spacing of the  $hkl$  reflection under the hydrostatic pressure  $P$ .

The crystal coordinate system  $K_C$  is defined by the (orthogonal) crystal axes. Microscopic physical relations, such as Hooke’s law relating the microscopic stress, strain, and single-crystal elastic moduli refer to each crystallite coordinate system  $K_C$ .  $d$  spacings for  $hkl$  reflections in individual grains should be extracted from calculations using Hooke’s law in  $K_C$ .

### 3. Texture and lattice preferred orientations

The texture in the sample can be represented by an orientation distribution function (ODF). The ODF is required to estimate anisotropic physical properties of polycrystals such as elasticity or plasticity.<sup>51</sup> The ODF represents the probability for finding a crystal orientation, and it is normalized such that an aggregate with a random orientation distribution has a probability of one for all orientations. If preferred orientation (texture) is present, some orientations have probabilities higher than one and others lower than one.

The ODF can be calculated using the variation in diffraction intensity with orientation using tomographic algorithms such as WIMW,<sup>52</sup> as implemented in the BEARTEX package<sup>53</sup> or in the “Maud Rietveld” refinement program.<sup>54</sup> This technique has been successfully applied to measure textures and deduce active high pressure deformation mechanisms.<sup>55</sup>

Textures of the sample analyzed here have been described in detail<sup>22</sup> and Fig. 3 presents inverse pole figures of the compression direction for experiment 2 at 3.5 and 42.6 GPa. For hcp-Co compressed in the DAC, we observe the development of a relatively strong texture with a maximum at about 15° from 0001.

### 4. Elastic strains

For polycrystals, diffraction peaks are the sum of the contribution from all crystallites in the correct reflection conditions, i.e., crystallites whose normal to the  $(hkl)$  plane is parallel to the scattering vector  $\mathbf{N}$ . The corresponding individual  $d$  spacings depend on the local stress and elastic properties in the grain considered. The measured  $d$  spacing



216  $d_m(hkl)$  is a weighted arithmetic mean of those individual  $d$   
217 spacings and corresponds to the 33 component of the elastic  
218 strain tensor in the diffraction coordinate system,  $K_D$  [Eq.  
219 (7)].

220 Theories have been developed to relate single-crystal  
221 elastic moduli to measured  $d$  spacings for stressed polycrys-  
222 tals. Most models rely on elasticity theory and assume either  
223 continuity of stress or of strain within the sample. If, in ad-  
224 dition, it is assumed that the sample is nontextured, it can be  
225 shown that the lattice strain can be expressed as<sup>14</sup>

$$226 \quad \epsilon_{33}^{p-K_D} = \frac{d_m(hkl) - d_p(hkl)}{d_p(hkl)} = Q(hkl)(1 - 3 \cos^2 \psi), \quad (8)$$

227 where  $\psi$  is the angle between the diffracting plane normal  
228 and the maximum stress direction ( $\mathbf{Z}_S$  in our case), and the  
229 lattice strain parameter  $Q(hkl)$  is a function of the differential  
230 stress  $t$  in the polycrystal and single-crystal elastic moduli  
231  $C_{ijkl}^p$ .

232 Theories that include texture effects have also been  
233 developed.<sup>56</sup> In this case, the measured  $d$  spacings do not  
234 vary linearly with  $(1 - 3 \cos^2 \psi)$  but can still be related to  
235 differential stress in the polycrystal and single-crystal elastic  
236 moduli. However, deviations between predictions of theories  
237 that include texture effects and those that neglect it are small  
238 and may be difficult to separate experimentally.<sup>57</sup> In any  
239 case, it has been shown that this theory does not apply to  
240 data measured on materials where plastic deformation takes  
241 place. In particular, these techniques yield inconsistent  
242 stresses and elastic constants for hcp-Co under  
243 pressure.<sup>21,22,58</sup>

## 244 C. Plastic model

### 245 1. EPSC model

246 The evolution of stress and strain with deformation ob-  
247 served in Co can be related to results of ambient pressure  
248 experiments on other hcp metals (i.e., Be, Mg, and Ti) un-  
249 dergoing plastic deformation which show a similar  
250 behavior.<sup>27,29,59,60</sup>  $hkl$ -dependent stresses deduced from lat-  
251 tice strains have already been documented and modeled for  
252 fcc metals and ionic solids with the NaCl structure using  
253 EPSC simulations.<sup>26,32,33</sup> In those simulations, certain  $hkl$   
254 reflections show a behavior close to that of a pure elastic de-  
255 formation, while others do not, displaying either larger or  
256 smaller effective stresses.

257 The EPSC model we use here<sup>31</sup> represents the aggregate  
258 by a discrete number of orientations with associated volume  
259 fractions. The latter are chosen such as to reproduce the ini-  
260 tial texture of the aggregate. EPSC treats each grain as an  
261 ellipsoidal elastoplastic inclusion embedded within a homo-  
262 geneous elastoplastic effective medium with anisotropic  
263 properties characteristic of the textured aggregate. The exter-  
264 nal boundary conditions (stress and strain) are fulfilled on  
265 average by the elastic and plastic deformations at the grain  
266 level. The self-consistent approach explicitly captures the  
267 fact that soft-oriented grains tend to yield at lower stresses  
268 and transfer load to plastically hard-oriented grains, which  
269 remain elastic up to rather large stress.

The model uses known values of single-crystal elastic 270  
moduli. The parameters associated with each plastic deformation 271  
mode are the critical resolved shear stresses (CRSS), 272  
given by a hardening evolution law. The simulated internal 273  
strains are compared to experimental data by identifying the 274  
grain orientations which, in the model aggregate, contribute 275  
to the experimental signal associated with each diffracting 276  
vector. 277

An EPSC simulation is based on applying stress or strain 278  
increments to the aggregate, depending on the boundary condi- 279  
tions, until the final deformation or stress state is achieved. 280  
At each step, stress and strain in each grain are incremented 281  
accordingly, as follows from its interaction with the effective 282  
medium representing the aggregate. The response of medium 283  
and grain is assumed to be described by a linear relation 284  
between stress and total strain increments, 285

$$\delta\sigma^c = L^c : \delta\epsilon^{c,\text{total}}, \quad (9) \quad 286$$

$$\delta\bar{\sigma} = \bar{L} : \delta\bar{\epsilon}^{\text{total}}, \quad (10) \quad 287$$

$$\delta\epsilon^{\text{total}} = \delta\epsilon^{\text{elastic}} + \delta\epsilon^{\text{plastic}}. \quad (11) \quad 288$$

Here  $\bar{L}$  is the elastoplastic stiffness of the aggregate and  $L^c$  289  
 $= C^c : (I - \sum_s m^s \otimes f^s)$  is the elastoplastic stiffness of the crystal. 290  
 $C^c$  is the single-crystal elastic tensor, and the sum is taken 291  
over the active slip systems  $s$  in the grain.  $m^s$  is the Schmid 292  
tensor which resolves the shear component of the stress or 293  
strain along a slip system and  $f^s$  is a tensor which relates 294  
stress and strain rates.<sup>61,62</sup> As more systems become plasti- 295  
cally active, the moduli  $L^c$  become more compliant. The 296  
stress equilibrium condition is solved for each grain assum- 297  
ing an ellipsoidal grain shape and using the Eshelby inclu- 298  
sion formalism. This procedure provides for a stress and 299  
strain increment in each grain. The macroscopic elastoplastic 300  
stiffness  $\bar{L}$  is derived iteratively by enforcing the condition 301  
that the polycrystal response has to be given by the weighted 302  
average of the individual grains responses and has to be con- 303  
sistent with the boundary conditions.<sup>31</sup> The main advantage 304  
of the EPSC model is that it allows for grains to deform 305  
more or less than the average, depending on their degree of 306  
hardening, their orientation, and their relative directional 307  
stiffness with respect to the medium. 308

### 2. Parameters and output of EPSC models 309

In our modeling of DAC RDX data, we assume that the 310  
sample was submitted to an axial compression along  $\mathbf{Z}_S$  in 311  
 $K_S$ . In all simulations, we assume that the sample consists of 312  
1000 randomly oriented spherical grains, with single-crystal 313  
elastic moduli and their pressure dependence taken from IXS 314  
measurements<sup>19</sup> (Table I). The polycrystalline sample is 315  
compressed in 3000 strain steps to a final state of strain de- 316  
fined by 317

$$\epsilon_x^{0-K_S} = -0.01 \quad 318$$

$$\epsilon_y^{0-K_S} = -0.01 \quad (12) \quad 319$$

TABLE I. Ambient pressure and first pressure derivative of elastic moduli of hcp-Co measured using IXS between 0 and 39 GPa (Ref. 19). In our simulation  $C_{ij}^P = C_{ij}^0 + P \cdot (\partial C_{ij} / \partial P)$ .

	$C_{11}$	$C_{33}$	$C_{12}$	$C_{13}$	$C_{44}$
$C_{ij}^0$ (GPa)	293	339	143	90	78
$\partial C_{ij} / \partial P$	6.1	7.6	3.0	4.2	1.38

320  $\epsilon_z^{0-K_S} = -0.17,$

321 where strains are expressed in  $K_S$  relative to dimensions un-  
 322 der ambient pressure. The deformation geometry was derived  
 323 from x-ray radiographs of the sample taken during the DAC  
 324 experiments<sup>63</sup> which indicate that our sample was submitted  
 325 to very little radial deformation. The final value of the axial  
 326 component  $\epsilon_z^{0-K_S}$  was chosen to match the simulated and ex-  
 327 perimental pressures at the end of the compression.

328 The model uses combinations of seven deformation  
 329 mechanisms typically found in hexagonal metals: slip of  
 330  $\frac{1}{3}\langle 11\bar{2}0 \rangle$ , or  $\langle a \rangle$  dislocations, on basal  $\{0001\}$ , prismatic  
 331  $\{10\bar{1}0\}$ , and pyramidal  $\{10\bar{1}1\}$  planes; slip of  $\frac{1}{3}\langle 11\bar{2}3 \rangle$ , or  
 332  $\langle c+a \rangle$  dislocations, on pyramidal  $\{10\bar{1}1\}$  or  $\{11\bar{2}2\}$  planes;  
 333 tensile twinning on  $\{10\bar{1}2\}$  planes; and, finally, compressive  
 334 twinning on  $\{11\bar{2}2\}$  planes (Table II). For each slip and twin  
 335 mode we describe the hardening of CRSS by means of an  
 336 empirical Voce hardening rule

337 
$$\tau = \tau_0 + (\tau_1 + \theta_1 \Gamma) \left\{ 1 - \exp\left(-\frac{\theta_0 \Gamma}{\tau_1}\right) \right\}, \quad (13)$$

338 where  $\tau$  is the instantaneous CRSS of the mechanism,  $\tau_0$  and  
 339  $\tau_0 + \tau_1$  are the initial and final back-extrapolated CRSS, re-  
 340 spectively,  $\theta_0$  and  $\theta_1$  are the initial and asymptotic hardening  
 341 rates, and  $\Gamma$  is the accumulated plastic shear strain in the  
 342 grain. Strain levels presented here are relatively low, so we  
 343 reduced the number of adjustable parameters by assuming  
 344 that  $\tau_1 = 0$ . In this case, the hardening law becomes linear  
 345 according to

346 
$$\tau = \tau_0 + \theta_1 \Gamma, \quad (14)$$

347 and only two adjustable parameters remain.

Output of the simulation includes the relative activity of 348  
 the various deformation mechanisms, the average stress in 349  
 the polycrystal, stress and strain within each grain of the 350  
 sample, and predicted lattice strains. The simulated elastic 351  
 lattice strains were compared to experimental data by iden- 352  
 tifying the model grains whose crystallographic planes are 353  
 oriented such as to contribute to the experimental signal. The 354  
 lattice strain (peak shift) is calculated as a weighted average 355  
 over all grains that contribute to the peak. Specifically, we 356  
 considered  $10\bar{1}0$ ,  $0002$ ,  $10\bar{1}1$ ,  $10\bar{1}2$ ,  $11\bar{2}0$ , and  $10\bar{1}3$  diffrac- 357  
 tion lines at  $\psi = 0, 15^\circ, 30^\circ, 45^\circ, 60^\circ, 75^\circ,$  and  $90^\circ$ . The 358  
 region of orientation space which contributes to the signal 359  
 was assumed to be within an interval of  $\pm 7.5^\circ$  with respect 360  
 to the diffraction vector. 361

3. Representation of simulated and experimental data 362

It has been shown that Eq. (8) does not apply to data 363  
 collected in RDX when samples are plastically deformed. 364  
 However, previous RDX experiments<sup>4,12,15,64-67</sup> have shown 365  
 that the measured  $d$  spacings are nearly linear when plotted 366  
 vs  $(1 - 3 \cos^2 \psi)$  and that the  $d$  spacings measured for  $\psi$  367  
 $= 54.7^\circ$  do correspond to those expected under the hydro- 368  
 static equivalent pressure. Therefore, experimental data were 369  
 reduced using 370

$$\epsilon_{33}^{P-K_D}(hkil, \psi) = \frac{d_m(hkil, \psi) - d_P(hkil)}{d_P(hkil)} = Q(hkil)(1 - 3 \cos^2 \psi), \quad (15) \quad 371 \quad 372$$

where  $d_m(hkil, \psi)$  is the measured  $d$  spacing for the  $hkil$  373  
 diffracting line at angle  $\psi$ ,  $d_P(hkil)$  is the  $d$  spacing for the 374  
 $hkil$  line under hydrostatic pressure  $P$ , and  $Q(hkil)$  is the 375  
 lattice strain parameter for the  $hkil$  line.  $d_P(hkil)$  and  $Q(hkil)$  376

TABLE II. List of deformation mechanisms used in the simulations.  $\tau_0$  and  $\theta_1$  are parameters for the simplified Voce hardening rule Eq. (14) and are expressed in GPa. Stars indicate deformation mechanisms that were not included in the final model.

Mechanism		Model 1		Model 2		Model 3		Model 4		Model 5	
		$\tau_0$	$\theta_1$	$\tau_0$	$\theta_1$	$\tau_0$	$\theta_1$	$\tau_0$	$\theta_1$	$\tau_0$	$\theta_1$
Basal	$\{0001\}\langle 1\bar{2}\bar{1}0 \rangle$	100	1	1	1	8	1	0.07	0.30	0.07	0.30
Prismatic	$\{10\bar{1}0\}\langle 1\bar{2}\bar{1}0 \rangle$	100	1	8	1	1	1	0.90	1.00	0.90	1.00
Pyramidal $\langle a \rangle$	$\{10\bar{1}1\}\langle 1\bar{2}\bar{1}0 \rangle$	100	1	100	1	100	1				
Pyramidal $\langle c+a \rangle$	$\{10\bar{1}1\}\langle 11\bar{2}3 \rangle$	100	1	100	1	100	1	0.70	1.50		
Pyramidal $\langle c+a \rangle$ second order	$\{11\bar{2}2\}\langle 11\bar{2}3 \rangle$										
Tensile twin	$\{10\bar{1}2\}\langle 10\bar{1}1 \rangle$										
Compressive twin	$\{2\bar{1}\bar{1}2\}\langle 2\bar{1}\bar{1}3 \rangle$									0.60	0.70

377 were adjusted to the experimental data.  $d_p(hkil)$  was then  
 378 used to estimate the average lattice parameters  $a$  and  $c$  of the  
 379 hexagonal crystal and the hydrostatic pressure  $P$  using a  
 380 known equation of state.<sup>36</sup> Experimental data for hcp-Co lat-  
 381 tice strains vs pressure obtained using such procedure are  
 382 extracted from Ref. 22 and summarized in Fig. 2.

383 The EPSC model calculates the average stress in the  
 384 sample,  $\sigma^{0-K_S}$ , from which we deduce the hydrostatic pres-  
 385 sure and differential stress

$$386 \quad P = (\sigma_{11}^{0-K_S} + \sigma_{22}^{0-K_S} + \sigma_{33}^{0-K_S})/3, \quad (16)$$

$$387 \quad t = \sigma_{33}^{0-K_S} - \left( \frac{\sigma_{11}^{0-K_S} + \sigma_{22}^{0-K_S}}{2} \right), \quad (17)$$

388 respectively. The EPSC model also provides absolute simu-  
 389 lated strains  $\epsilon_{33}^{0-K_D}(hkil, \psi)$  relative to  $d$  spacings under am-  
 390 bient pressure, which were used to calculate strains induced  
 391 by the hydrostatic pressure,  $\epsilon_p^0$ , and deviatoric lattice strains  
 392 parameters  $Q(hkil)$ . The procedure consists in fitting  $a$  and  $b$   
 393 parameters to

$$394 \quad \epsilon_{33}^{0-K_D}(hkil, \psi) = \frac{d_m(hkil, \psi) - d_0(hkil)}{d_0(hkil)} = a + b(1 - 3 \cos^2 \psi). \quad (18)$$

395 Using Eqs. (5) and (15), we get

$$396 \quad \epsilon_p^0 = \frac{d_p(hkil) - d_0(hkil)}{d_0(hkil)} = a, \quad (19)$$

$$397 \quad Q(hkil) = \frac{b}{1+a}. \quad (20)$$

#### 398 4. Pressure dependence of the elastic moduli

399 Since the original EPSC code did not include the effect of  
 400 pressure on elastic moduli, we modified it to calculate pres-  
 401 sure and update the corresponding elastic moduli, at each  
 402 step and in each grain. At each step  $i$ , the elastic strain in-  
 403 crement induced by the increment of stress applied to a grain  
 404 is calculated using

$$405 \quad \delta \epsilon_{kl}^{P-K_C}|_i = S_{klmn}^P [\sigma_{mn}^{0-K_C}|_i - \sigma_{mn}^{0-K_C}|_{i-1}], \quad (21)$$

406 where the coefficients  $S_{klmn}^P$  are elastic compliances, function  
 407 of the hydrostatic pressure in the grain at step  $(i-1)$ , and  
 408 stress tensors are absolute, relative to the state under ambient  
 409 pressure. Lattice spacing for each grain contributing to the  
 410 diffraction peak is then updated using

$$411 \quad d(hkil)|_i = d(hkil)|_{i-1} (1 + \delta \epsilon_{33}^{P-K_D}), \quad (22)$$

412 where  $\delta \epsilon_{33}^{P-K_D}$  is the component of the strain tensor  $\delta \epsilon_{kl}^{P-K_C}$   
 413 perpendicular to the diffracting plane.

414 The average lattice strain for each reflection and orienta-  
 415 tion to be compared with experimental data is then updated  
 416 by identifying the grains contributing to the diffraction and  
 417 calculating

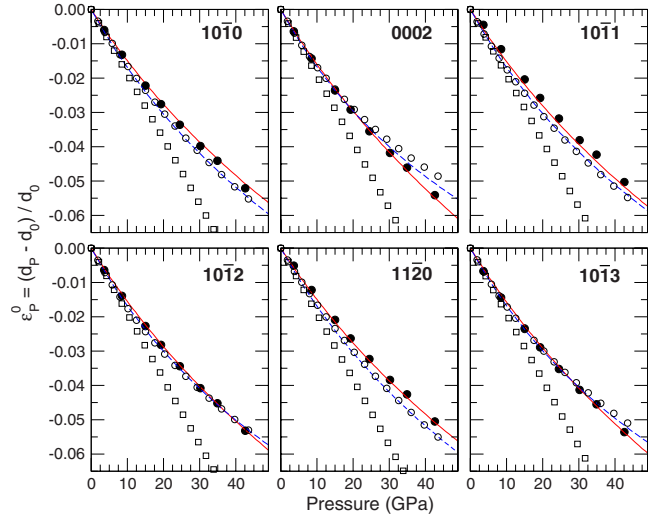


FIG. 4. (Color online) Measurement of hydrostatic strain vs pressure. Solid line is deduced from an equation of state measured under hydrostatic conditions (Ref. 36), dashed lines is deduced from the single-crystal elastic moduli measured using IXS (Ref. 19), black circles are measurement from radial x-ray diffraction (Ref. 22) at  $\psi=54.7^\circ$ , open squares are simulated using EPSC and no pressure dependence of elastic moduli, and open circles are results of EPSC models using the elastic moduli and their pressure dependence measured using IXS (Ref. 19).

$$418 \quad \epsilon^0(hkil) = \left[ \frac{d(hkil)|_i - d(hkil)|_0}{d(hkil)|_0} \right], \quad (23) \quad 419$$

420 where the average is taken over all grains contributing to the  
 421 diffraction.

### 422 III. RESULTS

423 In this section, we present simulations of the DAC experi-  
 424 ment done for hcp-Co using the EPSC model. In order to  
 425 study the effect of plasticity upon the lattice strain evolution,  
 426 we consider several combinations of active slip and twinning  
 427 modes, and several combinations of hardening parameters.  
 428 We will refer to each of these combinations as a crystal  
 429 model. The different sets and associated hardening param-  
 430 eters are listed in Table II. In all cases, we use the pressure  
 dependent elastic moduli for Co listed in Table I.

#### 431 A. Pressure dependence of elastic moduli and hydrostatic 432 equation of state

433 According to the elastic theory introduced earlier,  $d$  spac-  
 434 ings measured at  $\psi=54.7^\circ$  correspond to those associated  
 435 with the hydrostatic pressure  $P$  [see Eq. (15)]. While the  
 436 theory used to derive this result has strong limitations, nu-  
 437 merous RDX experiments have shown that equation of states  
 438 measured at this angle tend to correspond to those measured  
 439 under hydrostatic conditions.

440 Figure 4 presents the pressure dependence of  $\epsilon_p^0 = (d_p$   
 441  $- d_0)/d_0$  simulated with the EPSC model along with results  
 442 from RDX (Ref. 22) at  $\psi=54.7^\circ$ . The figure also shows  
 443 curves calculated using the bulk modulus and pressure de-

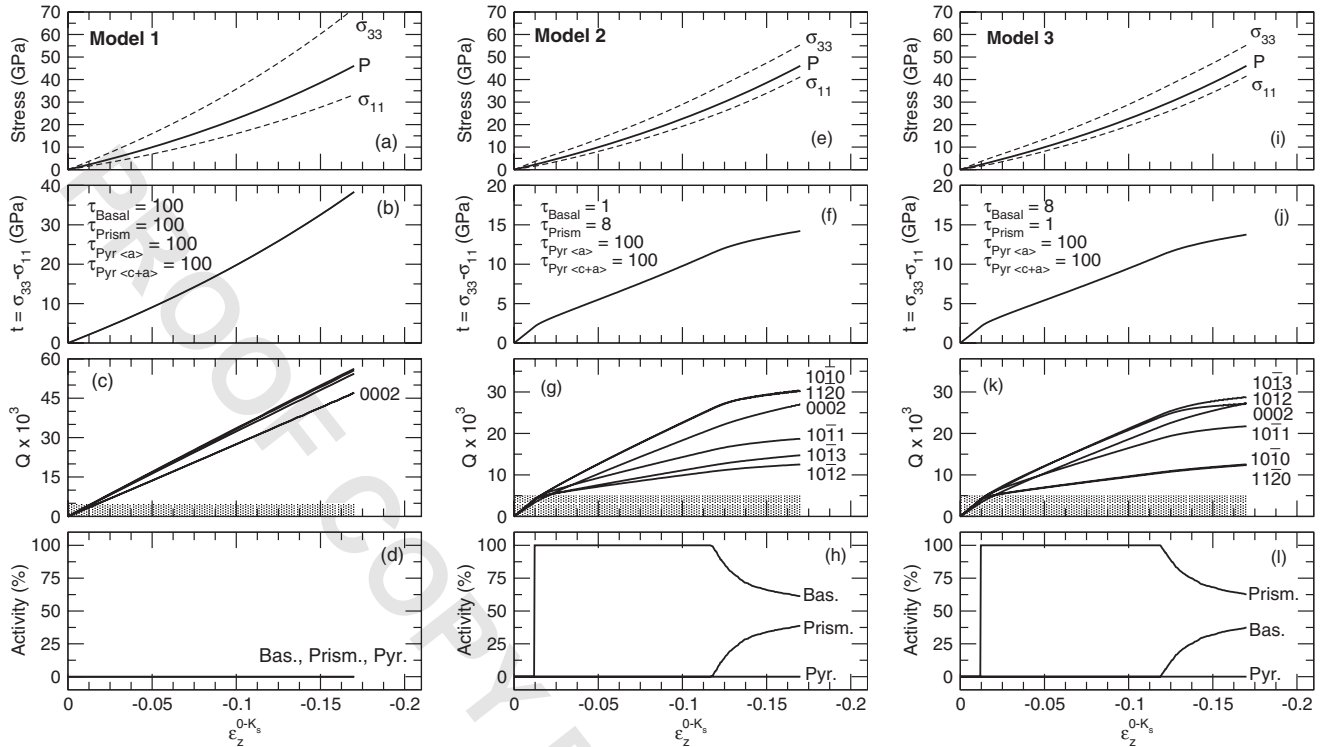


FIG. 5.  $\sigma_{11}$  and  $\sigma_{33}$  stress components, pressure [(a),(e),(i)], differential stress [(b),(f),(j)], lattice strain parameters [(c),(g),(k)], and relative activity of the deformation mechanisms [(d),(h),(l)], as a function of axial strain for simulations using models 1 [(a),(b),(c),(d)], 2 [(e),(f),(g),(h)], and 3 [(i),(j),(k),(l)] listed in Table II. In all cases, lattice strains simulated for the  $10\bar{1}0$  and the  $11\bar{2}0$  diffraction lines cannot be distinguished. For models 2 and 3 [Figs. 5(g) and 5(k)], Miller indices for which the lattice strains are calculated are labeled on the figure. For model 1, lattice strains for  $10\bar{1}0$ ,  $11\bar{2}0$ ,  $10\bar{1}1$ ,  $10\bar{1}2$ , and  $10\bar{1}3$  diffraction lines cannot be distinguished at this scale and are not labeled. Shaded area in Figs. 5(c), 5(g), and 5(k) indicates the order of magnitude of the experimental measurements. In all cases, pyramidal slip systems do not get activated. For model 1, none of the slip system gets activated and the simulation is fully elastic.

444 ppendence of the  $c/a$  ratio measured under hydrostatic  
 445 conditions<sup>36</sup> as well as compression curves calculated using  
 446 the single-crystal elastic moduli and their pressure depen-  
 447 dence measured using IXS (Ref. 19) that were assumed in  
 448 the calculation.

449 Compression curve calculated using the single-crystal  
 450 elastic moduli and their pressure dependence measured using  
 451 IXS differ slightly from those measured under hydrostatic  
 452 conditions. RDX results almost coincide with those deduced  
 453 from the hydrostatic equation of state, while EPSC results  
 454 almost coincide with those deduced from IXS measurements.  
 455 Small differences can be seen for  $10\bar{1}3$  and 0002 and they  
 456 will be discussed later. It is obvious from Fig. 4 how critical  
 457 it is, in this simulation, to account for the pressure depen-  
 458 dence of the elastic constants. Otherwise, predictions tend to  
 459 grossly overestimate the lattice strains as a function of pres-  
 460 sure.

461 **B. Effect of individual deformation mechanisms on the**  
 462 **simulated lattice strains**

463 Figure 5 presents the results of the EPSC calculations for  
 464 plasticity models 1, 2, and 3 (Table II). For each, we show  
 465 the evolution of the polycrystal stress components  $\sigma_{11}$  and  
 466  $\sigma_{33}$ , hydrostatic pressure  $P$ , differential stress  $t$ , the simulated  
 467 deviatoric lattice strain parameter  $Q(hkil)$ , and the deforma-

tion mechanisms relative activity as a function of the applied 468  
 axial strain  $\epsilon_z^{0-K_S}$ . 469

Pressure calculated as a function of  $\epsilon_z^{0-K_S}$  is independent 470  
 of the plasticity model used. For all cases, we obtain an 471  
 evolution of pressure with  $\epsilon_z^{0-K_S}$  compatible with predictions 472  
 based on the hydrostatic equation of state of hcp-Co. At the 473  
 end of our simulated compression, the sample volume is 474  
 reduced by 17% and pressure is 46.2 GPa. As demonstrated in 475  
 Fig. 5, all other results strongly depend on the plastic model 476  
 and they should be discussed independently. 477

For model 1, the strength of all deformation mechanisms 478  
 is purposely set too high for them to be activated. As a conse- 479  
 quence, the behavior of the polycrystal is fully elastic. The 480  
 differential stress and pressure in the sample increase contin- 481  
 uously with applied strain and  $t$  reaches a value of 38.3 482  
 GPa at a pressure of 46.2 GPa. The simulated lattice strain 483  
 parameters  $Q$  also increase continuously with pressure and 484  
 are about 1 order of magnitude higher than those measured 485  
 in the experiment [Figs. 2 and 5(c)]. 486

In model 2, basal slip is activated when the applied strain 487  
 reaches 0.0122. At this strain, pressure and differential stress 488  
 in the sample are 2.2 and 2.1 GPa, respectively. The activa- 489  
 tion of basal slip is correlated with a drop in the simulated 490  
 lattice strains for diffraction lines such as  $10\bar{1}1$ ,  $10\bar{1}2$ , and 491  
 $10\bar{1}3$ , corresponding to pyramidal planes, while lattice 492  
 strains for lines such as  $10\bar{1}0$ ,  $11\bar{2}0$ , and 0002, corresponding 493



494 to basal and prismatic planes, remain largely unaffected. The  
 495 activation of basal slip also coincides with a lower rate of  
 496 increase in the differential stress. Prismatic slip is activated  
 497 when  $\epsilon_z^{0-K_S}$  reaches 0.1170, corresponding to a pressure and  
 498 differential stress of 27.6 and 11.3 GPa, respectively. The  
 499 activation of prismatic slip correlates with a second inflec-  
 500 tion in the evolution of  $t$  with strain. Activation of prismatic  
 501 slip induces a drop in the simulated lattice strain for  $10\bar{1}0$   
 502 and  $11\bar{2}0$ , while strains for lines corresponding to basal  
 503 planes, such as 0002, remain largely unaffected. At the end  
 504 of the compression, differential stress reaches a value of 14.2  
 505 GPa at a pressure of 46.2 GPa.

506 In model 3, prismatic slip is activated when  $\epsilon_z^{0-K_S}$  reaches  
 507 0.0122. At this strain, pressure and differential stress in the  
 508 sample are 2.2 and 2.1 GPa, respectively. The activation of  
 509 prismatic slip is correlated with a drop in the simulated lat-  
 510 tice strains for diffraction lines such as  $10\bar{1}0$ ,  $11\bar{2}0$ , while  
 511 simulated lattice strains for lines corresponding to pyramidal  
 512 and basal planes remain largely unaffected. Basal slip is ac-  
 513 tivated when  $\epsilon_z^{0-K_S}$  reaches 0.1190, corresponding to a pres-  
 514 sure and differential stress of 28.2 and 11.1 GPa, respec-  
 515 tively. The activation of basal slip is correlated with a drop in  
 516 the simulated lattice strains for the lines such as  $10\bar{1}1$ ,  $10\bar{1}2$ ,  
 517 and  $10\bar{1}3$ , corresponding to pyramidal planes, while lattice  
 518 strains for lines corresponding to basal planes remain largely  
 519 unaffected. In all cases, activation of a plastic mode induces  
 520 a decrease in slope for  $t$  vs applied strain. At the end of the  
 521 compression, differential stress reaches a value of 13.7 GPa  
 522 at a pressure of 46.2 GPa.

523 We conclude from the above results that basal and pris-  
 524 matic slips split the strain evolution of the different diffrac-  
 525 tion lines, but do not reproduce the observed experimental  
 526 sequence. Also, basal activity relaxes strains in lines corre-  
 527 sponding to pyramidal planes, and prism activity in lines  
 528 corresponding to prismatic planes. In addition, although  
 529 basal and prismatic slips lower the predicted lattice strains in  
 530 comparison with the fully elastic model 1, they alone do not  
 531 provide enough relaxation resulting in simulated strains  
 532 larger than the measured ones. Since basal and prism slip do  
 533 not provide deformation along the  $c$  axis of the Co crystal,  
 534 we explore below the effect of the activation of crystallo-  
 535 graphic modes with a  $c$ -axis deformation component.

### 536 C. Optimized model

537 Models 4 and 5 (Table II) were found to best match the  
 538 experimental data (Figs. 1, 2, and 6). Among the typical  
 539 deformation mechanisms found in hcp metals, four were se-  
 540 lected: basal, prismatic, and either pyramidal  $\langle c+a \rangle$  slip or  
 541 compressive twinning. For both models, initial CRSS  $\tau_0$  and  
 542 hardening rate  $\theta_1$  were optimized to best match the measured  
 543 lattice strains and their evolution with pressure. Other  
 544 mechanisms, listed in Table II, were investigated but not in-  
 545 cluded in the final model. For instance, pyramidal  $\langle a \rangle$  slip  
 546 lowers lattice strains parameters  $Q$  for most lines except  
 547  $10\bar{1}3$  and 0002 and activation of tensile twinning separates  
 548 lattice strain parameters  $Q$  from  $10\bar{1}0$  and  $11\bar{2}0$ ; those effects  
 549 cannot be reconciled with the measured data.

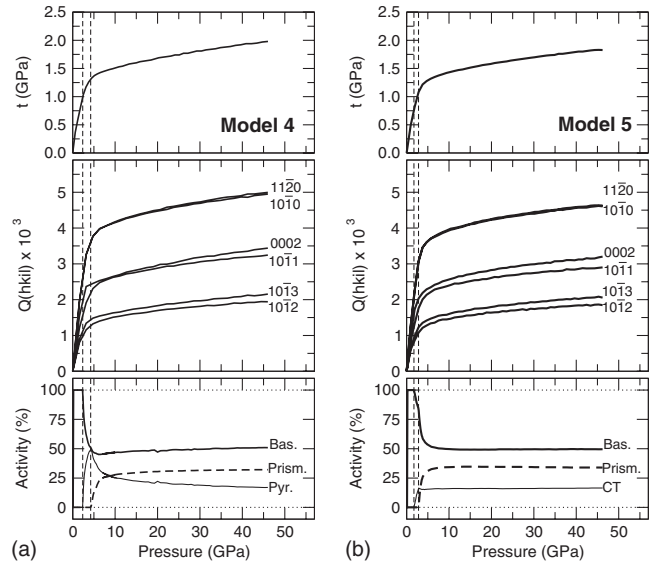


FIG. 6. Differential stress, lattice strain parameters, and relative activity of the deformation mechanisms as a function of pressure for simulations using models 4 and 5 in Table II. For model 4, vertical dashed lines at  $P=2.3$  GPa and  $P=4.3$  GPa correspond to the activation of pyramidal  $\langle c+a \rangle$  and prismatic slip, respectively. For model 5, vertical dashed lines at  $P=1.7$  GPa and  $P=2.8$  GPa correspond to the activation of compressive twinning and prismatic slip, respectively.

In both optimized models, the strength of basal slip  
 mostly controls lattice strains simulated for  $10\bar{1}1$ ,  $10\bar{1}2$ , and  
 $10\bar{1}3$ , while that of prismatic slip mostly influences  $10\bar{1}0$  and  
 $11\bar{2}0$  lattice strains. For model 4, 0002 lattice strains are  
 controlled by pyramidal  $\langle c+a \rangle$  slip, while in model 5, they  
 are controlled by the activation of compressive twinning.

Basal slip is by far the easiest slip system with an initial  
 CRSS of 0.07 GPa and a hardening coefficient of 0.3 GPa. In  
 both models, the relative strength of prismatic slip and com-  
 pressive twinning (model 5) or pyramidal slip (model 4)  
 were adjusted to start prismatic slip last and eventually take  
 over the deformation (Fig. 6). This was important to properly  
 reproduce the measured 0002 lattice strains which are on the  
 same order of magnitude that those of  $10\bar{1}0$  and  $11\bar{2}0$  early  
 in the compression and saturate later on.

In model 4, basal slip is activated at  $P=0.2$  GPa, with  $t$   
 $=0.2$  GPa. Pyramidal slip is activated when the pressure and  
 differential stress are 2.3 and 1.0 GPa, respectively. Finally,  
 prismatic slip is activated when  $P=4.3$  GPa and  $t$   
 $=1.3$  GPa. At the end of the compression, the differential  
 stress reaches 2.0 GPa at a pressure of 46.2 GPa.

In model 5, basal slip is activated at  $P=0.2$  GPa, with  $t$   
 $=0.2$  GPa. Compressive twinning is activated when the  
 pressure and differential stress are 1.7 and 0.8 GPa, respec-  
 tively. Finally, prismatic slip is activated when  $P=2.8$  GPa  
 and  $t=1.0$  GPa. At the end of the compression, the differ-  
 ential stress reaches 1.8 GPa at a pressure of 46.2 GPa.

### D. Plasticity and texture evolution

Slip and twinning induce grain reorientation and, as a  
 consequence, texture evolution. In our experiments we start



580 from a random aggregate of Co crystals and finish with a  
581 textured aggregate, where the  $c$  axis shows a tendency to  
582 align with the compression direction. This confirms that plas-  
583 tic deformation takes place during the DAC test. What re-  
584 mains to be tested is whether the experimental texture is  
585 consistent with compressive twinning or  $\langle c+a \rangle$  slip activity,  
586 as models 4 and 5 predict, respectively.

587 The EPSC code that we use here does not account for  
588 grain reorientation associated with plastic deformation and  
589 cannot be used to simulate texture evolution. Similarly to our  
590 EPSC model, the viscoplastic self-consistent (VPSC) code<sup>68</sup>  
591 treats each grain as a viscoplastic inclusion in a homoge-  
592 neous matrix that has the average properties of the polycrys-  
593 tal and can be used for texture simulations. Starting with an  
594 initial distribution of crystallite orientations and assuming  
595 deformation by slip and twinning, we can simulate a defor-  
596 mation path by enforcing incremental deformation steps. As  
597 deformation proceeds, crystals deform and rotate to generate  
598 preferred orientation. In VPSC calculations, the elastic re-  
599 sponse of the polycrystal is neglected, but grain rotations are  
600 properly accounted for, and this code has been used multiple  
601 times to model and understand textures obtained in DAC  
602 RDX experiments.<sup>55</sup>

603 A limitation of VPSC in connection with this work is that  
604 VPSC is based on an incompressible constitutive law, and  
605 calculations should be run at constant volume, that is with  
606  $(\epsilon_x + \epsilon_y + \epsilon_z) = 0$ . According to the equation of state, volumet-  
607 ric strain imposed by compressing polycrystalline cobalt to a  
608 pressure of 46 GPa is 17%, corresponding to axial strains of  
609 5.7%. In the actual sample, 5.7% of the applied axial strain  
610  $\epsilon_z^{0-K_S}$  is accommodated elastically and the remaining 11.3%  
611 plastically, increasing stress in the radial directions  $\sigma_x$  and  
612  $\sigma_y$ . We ran the VPSC calculations with strains corresponding  
613 to the actual plastic deformation applied to the DAC sample,  
614 which is to a maximum axial strain of 10% while preserving  
615  $\epsilon_x + \epsilon_y = -\epsilon_z$ .

616 We used the parameters of models 4 and 5 in Table II to  
617 model the development of texture in polycrystalline cobalt  
618 deformed in the DAC. Simulations were performed in 200  
619 steps, starting with a randomly oriented sample of 1000  
620 grains assuming an effective interaction between grains. A  
621 viscoplastic linear hardening Voce law was used. Activity of  
622 slip systems in all 1000 grains is evaluated in each of the  
623 steps and orientations are updated accordingly. From the ori-  
624 entation distribution of 1000 grains, inverse pole figures  
625 were calculated to illustrate crystal orientation patterns. All  
626 texture processing has been performed with the software  
627 Beartex.<sup>53</sup>

628 In both cases, we obtain a well defined texture with a  
629 maximum located near 0001, that is, with the basal planes  
630 perpendicular to the compression direction [Figs. 3(c) and  
631 3(d)]. After 10% strain, the inverse pole figures of the com-  
632 pression direction have a maximum of 2.20 and 2.22 mul-  
633 tiples of a random distributions (m.r.d.) for VPSC calcula-  
634 tions using models 4 and 5, respectively. Differences can be  
635 seen in the exact location of the maximum. In the experimen-  
636 tal data, the texture component is evenly spread at about 15°  
637 of the  $c$  direction. Simulations using model 4 give a maxi-  
638 mum at about 15° of the  $c$  direction and centered around  
639  $(10\bar{1}l)$  planes. For model 5, this maximum is located at about

15° of the  $c$  direction and centered around  $(11\bar{2}l)$  planes. 640

It should be noted that the 15° shift of the  $c$  direction in 641  
the inverse pole figure cannot be attributed to experimental 642  
errors and is clearly visible in the measured variations in 643  
diffraction intensities with orientation (e.g., Fig. 3 in Ref. 644  
22). It is also well reproduced by VPSC calculations. It 645  
should also be noted that textures measured in hcp-Fe do not 646  
always show a full alignment of the  $c$  axes with the compres- 647  
sion direction<sup>69,70</sup> and that a shift of the maximum from the  $c$  648  
direction has been observed in hcp-Fe.<sup>70</sup> 649

The conclusion of this calculation is that, although the 650  
VPSC predicted textures were obtained by enforcing only 651  
the plastic component of strain, they show that both pyrami- 652  
dal  $\langle c+a \rangle$  slip and compressive twinning activity are consis- 653  
tent with the texture measured experimentally in the DAC 654  
for Co. 655

## IV. DISCUSSION 656

### A. Validity of lattice strain parameters $Q$ 657

In Sec. II C 3 we assumed that the experimental data 658  
could be adjusted to Eq. (15). This implies that the  $d$  spac- 659  
ings measured at  $\psi=54.7^\circ$ ,  $d_p(hkil)$ , correspond to those as- 660  
sociated with the hydrostatic pressure, and that the effect of 661  
differential stress can be summarized in the form of one 662  
unique lattice strain parameter  $Q$ . 663

Experimental data indicate that equation of states mea- 664  
sured on stressed samples at  $\psi=54.7^\circ$  do agree with those 665  
measured under quasihydrostatic conditions. Results of 666  
EPSC calculations support this observation as the hydrostatic 667  
strains adjusted to Eq. (15) do not depend significantly on the 668  
combination of activated plastic deformation mechanisms. In 669  
our models, small deviations can be observed between the 670  
calculated hydrostatic strains and those expected from the 671  
single-crystal elastic moduli, e.g., 0002 and  $10\bar{1}3$  in Fig. 4, 672  
but those are significantly lower than typical errors due to 673  
differential stress. Therefore, our model supports the idea 674  
that equation of states measurements at  $\psi=54.7^\circ$  on stressed 675  
samples are a valid alternative if no better solution for reduc- 676  
ing the deviatoric stress can be found. 677

The assumption that the measured  $d$  spacings vary lin- 678  
early with  $(1-3\cos^2\psi)$  and can be summarized with a 679  
single parameter  $Q$  is more questionable. In the case of Co,  $d$  680  
spacings measured for  $11\bar{2}0$  do not follow this relation. The 681  
use of the lattice strain parameters  $Q$  is useful to compare 682  
experimental data and output of EPSC models. However, the 683  
model predictions should be compared against actual mea- 684  
sured  $d$  spacings, as shown in Fig. 1. In this figure we dem- 685  
onstrate that both models 4 and 5 can correctly reproduce the 686  
essentially nonlinear experimental curves. 687

In the experimental data, we observe a split of lattice 688  
strains measured for 0002 and 0004 above 25 GPa (Fig. 2). 689  
This cannot be accounted for using the model presented here 690  
as strains calculated to 0002 will be equal to those calculated 691  
for 0004. This observation will have to be confirmed and 692  
modeled in further studies. 693

### B. Average pressure and stress in the polycrystalline sample 694

It is interesting to note that the evolution of pressure with 695  
applied strain does not depend on the proposed plastic model 696

697 (e.g., Fig. 5). Plastic deformation occurs at constant volume  
698 and is independent of pressure. As a consequence, it has no  
699 influence on the relation between the applied axial strain and  
700 the average pressure within the sample.

701 Axial stresses, on the other hand, show a very different  
702 behavior. At the highest compression, pure elastic compress-  
703 sion results in an axial stress  $\sigma_{33}=71.6$  GPa and radial stress  
704  $\sigma_{11}=\sigma_{22}=33.3$  GPa [Fig. 5(a)]. For optimized plastic mod-  
705 els 4 and 5, we find  $\sigma_{33}=47.5(1)$  GPa and  $\sigma_{11}=\sigma_{22}$   
706  $=45.5(1)$  GPa.

707 Plastic deformation results in a redistribution of stress in  
708 the polycrystalline sample. Grains that deform plastically  
709 change the stress balance of the polycrystal, decreasing the  
710 average stress supported by the polycrystal in the axial di-  
711 rection while increasing the stress supported in the radial  
712 direction.

713 The evolution of differential stress with pressure is very  
714 similar for both optimized models (Fig. 6). In both cases, we  
715 find a fast increase in differential stress to 1.3 GPa at a pres-  
716 sure of 5 GPa. At 42.6 GPa, differential stress for models 4  
717 and 5 are 2.0 and 1.8 GPa, respectively. The value of 1.3  
718 GPa corresponds to stresses where all important deformation  
719 mechanisms are activated and could be qualified as yield  
720 strength for the present sample. Increase in differential stress  
721 between 1.3 and 1.9 GPa at higher pressures is related to a  
722 pressure-induced increase in elastic constants as well as  
723 strain hardening in the sample.

### 724 C. Strength and deformation mechanisms activities

725 Both optimized models 4 and 5 predict a very low  
726 strength and high activity of basal slip for hcp-Co, in line  
727 with observations under ambient pressure.<sup>40,42</sup> This is re-  
728 quired to reproduce the observed relatively low lattice strains  
729 for pyramidal diffraction lines such as  $10\bar{1}1$ ,  $10\bar{1}2$ , or  $10\bar{1}3$ .  
730 Lattice strains for those planes are extremely sensitive the  
731 values of the parameters  $\tau_0$  and  $\theta_1$  of the Voce hardening  
732 rule.

733 We also predict a relatively low strength and high activity  
734 for prismatic slip. This is required to match the observed  
735 lattice strains for  $10\bar{1}0$  and  $11\bar{2}0$ . Prismatic slip is commonly  
736 observed in metals with the hcp structure and has been re-  
737 ported in Co.<sup>44</sup> The lattice strains above are extremely sen-  
738 sitive to  $\tau_0$  and  $\theta_1$  for prismatic slip.

739 Models 4 and 5 differ in the activation of pyramidal  $\langle c+a \rangle$   
740 slip or compressive twinning, respectively. Compressive  
741 twinning has been reported in cobalt in the literature,<sup>40,43</sup>  
742 whereas observations of pyramidal  $\langle c+a \rangle$  slip are scarce. Ex-  
743 perimentally measured textures show a maximum evenly  
744 spread at about  $15^\circ$  of the  $c$  direction. VPSC simulations  
745 using model 4 show a maximum at about  $15^\circ$  of the  $c$  direc-  
746 tion and centered around  $(10\bar{1}l)$  planes. For model 5, this  
747 maximum is located at about  $15^\circ$  of the  $c$  direction and cen-  
748 tered around  $(11\bar{2}l)$  planes. This suggests that a full model  
749 accounting for the plastic deformation of hcp-Co should  
750 probably include a combination of both pyramidal  $\langle c+a \rangle$  and  
751 compressive twinning. In the future, we expect to be able to  
752 resolve this issue by repeating our simulations using an im-

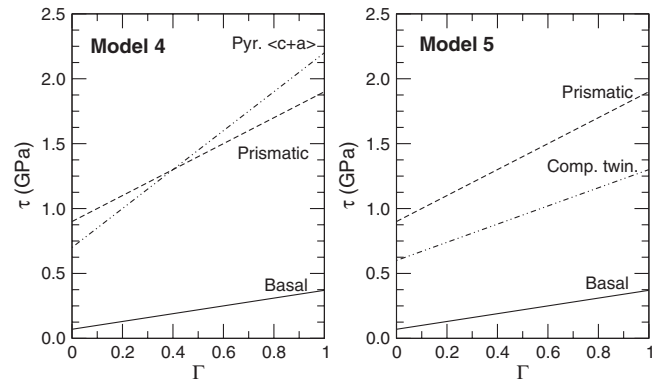


FIG. 7. Absolute CRSS of each active deformation mechanism as a function of accumulated plastic shear strain in the grain for models 4 and 5 in Table II.

proved version of EPSC with slip and twin reorientation. 753

In both optimized simulations, activation of pyramidal 754  
 $\langle c+a \rangle$  slip or compressive twinning controls lattice strains 755  
for the 0002 diffraction line. Voce law parameters were opti- 756  
mized to force activation of either  $\langle c+a \rangle$  slip or compres- 757  
sive twinning before activation of prismatic slip. Large hard- 758  
ening coefficients were necessary for both mechanisms to 759  
ensure a later activation of prismatic slip. In all cases, acti- 760  
vation of prismatic slip prior to pyramidal  $\langle c+a \rangle$  slip or com- 761  
pressive twinning resulted in models that do not fit the ex- 762  
perimental data. 763

Figure 7 presents the absolute CRSS of each active defor- 764  
mation parameter as a function of accumulated plastic shear 765  
strain in the grain  $\Gamma$  for models 4 and 5 in Table II. For basal 766  
slip,  $\Gamma$  can reach values as high as 4 in some grains at the end 767  
of the simulation. For other deformations modes, final values 768  
of  $\Gamma$  range between 0.8 and 2, depending on grains and de- 769  
formation mechanisms. The hardening law we used does not 770  
account for an effect of pressure on the CRSS and all experi- 771  
mental data could be fit using the simple, linear, strain de- 772  
pendent hardening law shown in Fig. 7. More experiments, 773  
where plastic deformation of the sample starts later in the 774  
compression rather than ambient pressure, will be required to 775  
quantify an effect of pressure on plasticity, but we could not 776  
extract such information from the present data. 777

### 778 D. Stress heterogeneities within the polycrystal

Figure 6 presents the evolution of the average differential 779  
stress as a function of pressure for models 4 and 5 while Fig. 780  
8 shows histograms of the distribution of pressure, differen- 781  
tial stress  $t=\sigma_{33}-(\sigma_{11}+\sigma_{22})$ , and lateral stress  $(\sigma_{22}-\sigma_{11})$  782  
among grains in the sample at the end of compression for 783  
both models. Pressure is very uniform and only varies by 784  
0.05 GPa from grain to grain, which is on the order of mag- 785  
nitude of numerical errors in the calculation. Distributions of 786  
differential and lateral stress, however, are not uniform and 787  
model dependent. 788

Lateral stresses show a distribution centered around 0 789  
GPa, as expected. For both models, minimum and maximum 790  
lateral stresses among grains are of the same order of mag- 791  
nitude than the average differential stress in the sample. 792

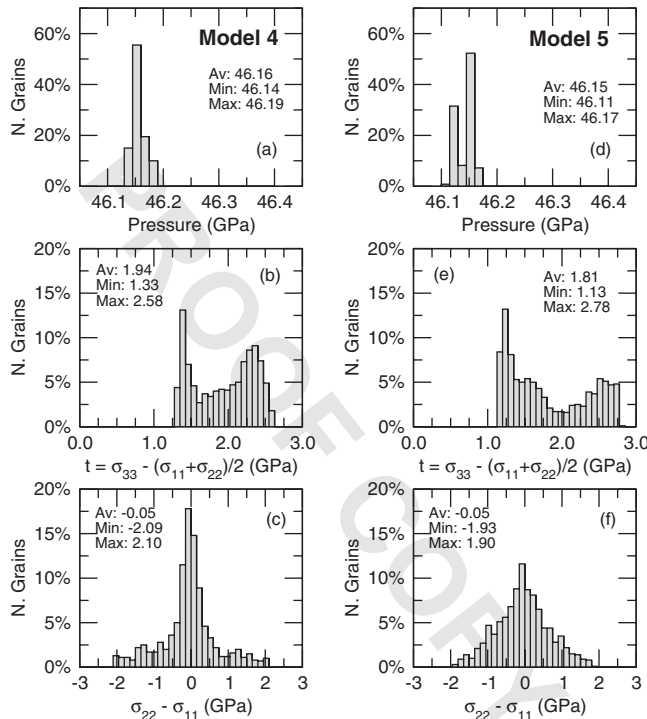


FIG. 8. Histograms of the distribution of pressure, differential stress, and lateral stress among grains in the sample at  $P = 46.2$  GPa for EPSC calculations using models 4 [(a),(b),(c)] and 5 [(d),(e),(f)] in Table II.

793 For both models, differential stress among grains shows a  
794 bimodal distribution whose mean corresponds to the average  
795 differential stress in the polycrystalline sample. Differences  
796 between the minimum and maximum stress among grains is  
797 lower than the average differential stress but well over 1  
798 GPa. Two grain families can be identified: grains in soft ori-  
799 entations that were submitted to large plastic deformation  
800 and show a relatively low differential stress, and grains in  
801 hard orientations that were submitted to less plastic deforma-  
802 tion and show a relatively high differential stress.

803 The relevant conclusion of the stress distribution analysis  
804 is that plasticity leads to a significant spread of stress among  
805 grains. This explains why models based on assuming uni-  
806 form states in the aggregate<sup>14</sup> yield inconsistent stresses and  
807 elastic constants for materials deforming plastically.<sup>21,22,32,33</sup>  
808 Figure 8 demonstrates that, as slip or twinning is activated  
809 inside a grain, deviatoric stresses are relaxed within the  
810 grain, and the state of stress among grains in the aggregate  
811 becomes very heterogeneous. This cannot be accounted for  
812 with theories relying solely on continuum mechanisms and  
813 numerical models such as those presented here should be  
814 applied.

#### 815 E. Limitations of the model

816 As demonstrated in this paper, EPSC models are very  
817 successful for understanding and modeling internal stress  
818 and strain in plastically deforming polycrystals. The current  
819 approach, however, has limitations. They can be separated in

two categories: limitations of the self-consistent approach,  
and limitations of the actual code we used.

The self-consistent model treats each grain as an ellipsoi-  
dal elastoplastic inclusion embedded within a homogeneous  
elastoplastic effective medium. As such, local interactions  
from grain to grain and heterogeneities within the grains  
themselves are not accounted for. Three-dimensional (3D)  
full-field polycrystalline models can predict local-field  
variations.<sup>71-73</sup> These calculations show important heteroge-  
neities within grains and a strong localization of stress and  
strain near the grain boundaries. However, the precision of  
those models comes with large computational cost and com-  
plexity, and they cannot be systematically applied for inter-  
preting experimental results. Mean-field approaches such as  
EPSC models are very successful and currently remain most  
convenient to explore and understand experimental results.<sup>73</sup>

The EPSC code we used did not account for grain reori-  
entation associated with slip and twinning deformation.  
While we do not expect that texture evolution will change  
the qualitative conclusions of this paper concerning the type  
and role of deformation mechanisms, we do expect that it  
will influence CRSS and hardening parameters. In the cur-  
rent version of the model, grains that have an orientation  
favorable for the activation of a deformation mechanism will  
be activated at each step. In reality, those grains should rotate  
and finally reach orientations less favorable for the deforma-  
tion mechanism. As such, we expect the hardening param-  
eters reported in Table II to be slightly overestimated.

## V. CONCLUSIONS

A modification of the EPSC model of Turner and Tomé<sup>31</sup>  
was used to successfully model x-ray diffractions measure-  
ments performed on hcp-Co samples plastically deformed  
under high pressure. Important information provided by the  
model includes: actual values of differential stress in the  
polycrystal, stress distribution among grains in the sample,  
as well as identification, relative activity, and strength of the  
active deformation mechanisms.

The model confirms that the effect of differential stress  
and plastic deformation on measured  $d$  spacings is often  
minimal at  $\psi = 54.7^\circ$ . Therefore, measurements of  $d$  spacings  
at this angle can be used to estimate hydrostatic equation of  
states if no better solution is available. This is particularly  
applicable to measurements above 100 GPa for which no  
hydrostatic pressure transmitting medium is available.

We find that the plastic behavior of hcp-Co plastically  
deformed under high pressure is controlled by basal and pris-  
matic slip of  $\langle a \rangle$  dislocations, and either pyramidal slip of  
 $\langle c+a \rangle$  dislocations or compressive twinning. Strength and  
hardening coefficients for those mechanisms have been de-  
termined and are listed in Table II. Basal slip is by far the  
easiest and most active deformation mechanism, with an ini-  
tial strength of 0.07 GPa and a linear hardening coefficient of  
0.30 GPa.



**873** For hcp-Co deformed axially in the diamond-anvil cell,  
**874** we observe a fast increase in differential stress to 1.3 GPa  
**875** between pressures of 0 and 5 GPa. The later part of the  
**876** compression shows a slower increase in differential stress  
**877** with pressure. At 42 GPa, the differential stress in hcp-Co is  
**878**  $1.9 \pm 0.1$  GPa. The transition between the fast and slow in-  
**879** crease in differential stress in the sample is related to the  
**880** sequential activation of plastic deformation mechanisms in  
**881** the sample.

EPSC models are very powerful and overcome many **882**  
 limitations of models based on continuum elasticity theory **883**  
 for the interpretation of x-ray diffraction data measured on **884**  
 stressed samples. They should be used for the interpretation **885**  
 of all high pressure deformation experiments where x-ray **886**  
 diffraction is used to probe stress within a polycrystalline **887**  
 sample. **888**

**889**  
**890**  
**891**

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## AUTHOR QUERIES —

- #1 AU- PRB does not allow claims of novelty. Please check replacement of “introduce” with “discuss”
- #2 AU- Please supply definition for the acronym “WIMW” if possible
- #3 AU- Please check deletion of “\*” in Table II
- #4 AU-Although a caption makes reference to color online, figures will appear black and white in print. Please make sure the caption makes sense to print reader
- #5 CrossRef reports the volume should be ‘34’ not ‘34A’ in the reference 30 ‘Brown, Bourke, Clausen, Holden, Tome, Varma, 2003’.
- #6 CrossRef reports the year should be ‘1955’ not ‘1954’ in the reference 38 ‘McSkimin, 1954’.
- #7 AU- Please verify the journal title of Ref. 48
- #8 AU- Please verify the journal title of Ref. 54
- #9 CrossRef reports the author should be ‘A. Lebensohn’ not ‘Lebensohn’ in the reference 72 ‘Lebensohn, 2001’.